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Highlights

- The width of a fluid jet in a rectangular microchannel follows a universal power law.
 - Microcapsules can be sorted by size at low flow strength.
 - Microcapsules can be sorted by deformability at high flow strength.
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Medical Engineering and Physics

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Deformability- and size-based microcapsule sorting

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ARTICLE INFO

Article history:

Received 19 January 2017

Revised 20 June 2017

Accepted 25 June 2017

Available online xxx

MSC:

00-01

99-00

Keywords:

Microfluidics

Capsule

Deformability

Separation

ABSTRACT

Biomedical applications often require to sort cells according to their physical properties, such as size, density or deformability. In recent years, microfluidics has provided a variety of tools to sort micro-objects. We present here a simple microfluidic device consisting of a channel containing a semi-cylindrical obstacle against which capsules are squeezed by the flow, followed by a diverging chamber where streamlines separate. We demonstrate that this basic system is capable of sorting elastic microcapsules according to their size at low flow strength, and according to the stiffness of their membrane at high flow strength. While most existing devices exhibit their best performances when the size or deformability contrast is maximal, we show that our device is capable of discriminating between capsules whose membrane elasticity differs by a factor of order unity.

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1. Introduction

The shape and mechanical properties of blood cells govern many important phenomena, such as margination [1], adhesion [2], and extravasation [3]. Pathologies such as cancer [4] or infections [5] may alter cell size and stiffness. Abnormal stiffness can be used as a sorting parameter in the detection and isolation of pathological cells [6].

Microfluidics presents many advantages for cancer diagnosis applications, such as small reaction volumes, high sensitivity, and ability to sort micro-objects (particles, capsules, and cells) as described in [7]. Among label-free separation techniques, the most studied are size-based sorting devices: deterministic lateral displacement [8,9], dielectrophoresis [10], hydrophoresis [11], acoustic waves [12,13], and inertia [14]. Other methods based on chemical properties sort micro-objects thanks to the composition of their membrane, such as immunocapture [15] and fluorescence-activated sorting [16]. Finally, other techniques such as optical stretchers [17] and stiffness-dependent separation [18] can sort heterogeneous populations based on their mechanical properties. While size-based microfluidic sorting has already been studied

extensively [19], the concept of sorting based on deformability has emerged more recently and proves very promising [18,20].

In bioengineering, particles, capsules and vesicles are considered as simplified models for cells [21–23]. Capsules are biomimetic micro-objects consisting of a thin elastic membrane reticulated around a liquid core. The membrane can be made of natural components such as proteins: human serum albumin (HSA) [24], or ovalbumin [25]. The behavior of capsules is studied under conditions mimicking physiological situations, such as flowing through a constriction [26], and in the context of drug encapsulation and delivery [27].

The influence of confinement has been extensively studied for millimetric and micrometric capsules flowing through cylindrical [25], square [28], or rectangular channels [29].

In a recent numerical study, Zhu et al. [30] proposed to sort elastic capsules based on their deformability by flowing them around an obstacle through a straight channel followed by a diverging chamber. The experimental validation of deformability-based sorting techniques is not trivial because of the lack of homogeneous populations of micro-objects with well-controlled stiffness. We have created a microfluidic device with such a geometry. We use spherical albumin microcapsules whose mechanical properties depend on the production conditions.

In this article, we evaluate the feasibility of experimentally sorting heterogeneous populations of microcapsules depending on their stiffness.

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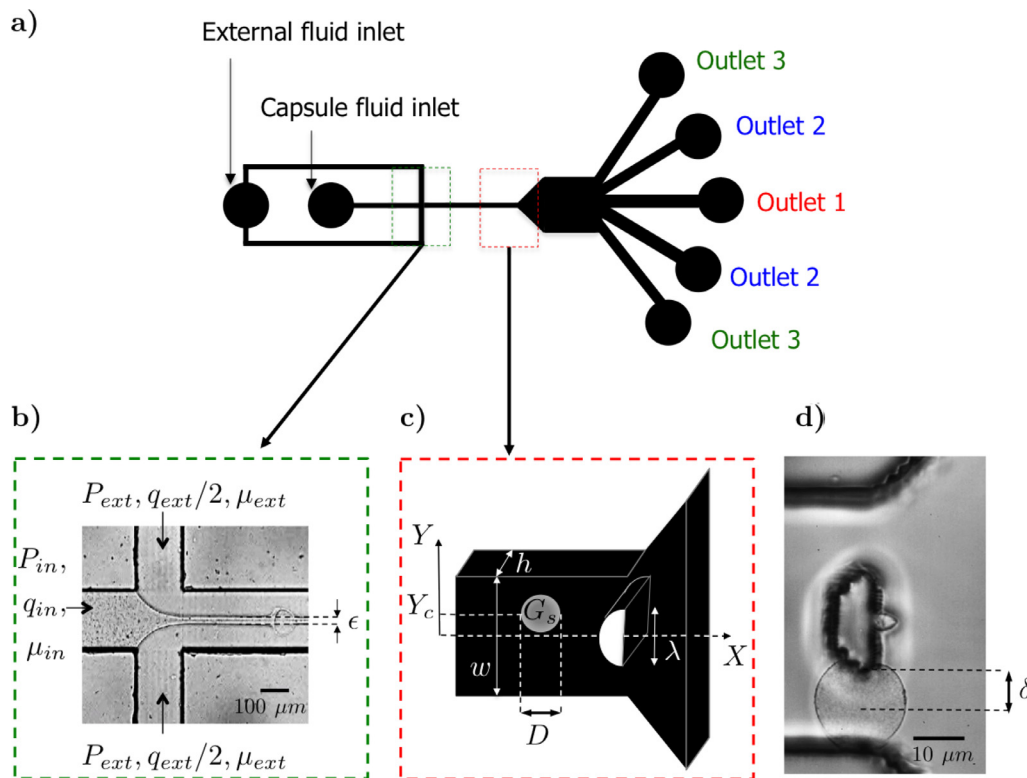


Fig. 1. Sketch of the experimental device. The fluids flow from left to right. (a) General view of our sorting device. (b) Photograph of the flow-focusing at the entrance of the straight channel. The capsule suspension is pinched by an external viscous fluid of viscosity μ_{ext} , and forms a fluid thread of viscosity μ_{in} and thickness ϵ . (c) Dimensions of the obstacle and of the rectangular straight channel. (d) The distance between the center of mass of the capsule and the obstacle is defined as δ .

47 2. Materials and methods

48 2.1. Capsule suspensions

49 Capsules are prepared by interfacial cross-linking as described
 50 elsewhere [31]. Briefly, a water-in-oil emulsion is formed using a
 51 10% ovalbumin solution in a phosphate buffer pH 5.9 or pH 8,
 52 dispersed in cyclohexane added with 2% m/V sorbitan trioleate.
 53 Adding 2.5% (w/v) terephthaloyl chloride to the organic phase induces
 54 ovalbumin cross-linking at the interface and the formation
 55 of the membrane. This chemical reaction is stopped by dilution
 56 with chloroform:cyclohexane (1:4, v/v) after 5 min. Capsules are
 57 then rinsed with an aqueous solution of polysorbate, then with
 58 pure water, resuspended in water and stored at 4 °C. We obtain
 59 a polydisperse population of capsules of diameter D , determined
 60 with the Image J software using a circular fit, and expressed as the
 61 mean \pm the standard deviation. The deformability of capsules obtained
 62 by this protocol has been shown to depend on the pH of the
 63 buffer solution containing ovalbumin. Capsules prepared at higher
 64 pH are more rigid than those prepared in more acidic conditions
 65 [25]. Capsule stiffness is characterized by the 2D elastic shear modulus
 66 of the membrane G_s .

67 2.2. Microfluidic device

68 The sorting device (Fig. 1) consists of a straight rectangular
 69 channel of width w and depth h that contains a semi-cylindrical
 70 obstacle of diameter λ at its end (Fig. 1c). Upstream of the main
 71 channel, a flow-focusing module is added to focus the capsules
 72 onto the center of the obstacle (Fig. 1). Downstream of the obstacle,
 73 the channel widens (Fig. 1a), then splits into several exits. The
 74 width of the confined zone between the side wall and the obstacle
 75 was chosen to be smaller than the capsule size (Fig. 1d). We define

as δ the distance between the center of mass of the capsule and
 the pillar. 76 77

78 2.3. Production of the microfluidic device

79 Microfluidic chips are produced in PDMS using standard soft
 80 lithography techniques [32]. PDMS and curing agent (Sylgard) are
 81 mixed in a 10:1 ratio and cast onto the master, which consists of
 82 a silicon wafer with SU8-photosensitive microstructures (Microfactory,
 83 Paris). After baking for 2 h at 70 °C, the PDMS is cross-linked and
 84 can be peeled off from the SU8 master. It is then plasma-bonded
 85 together with a glass slide using air plasma generated by a plasma-
 86 oxidizer (HARRICK, NY 14850, USA). After 2 h in a stove at 70 °C,
 87 the device is ready to be used.

88 2.4. Experimental setup

89 The sketch of our experimental setup is shown in Fig. 1. A pres-
 90 sure controller (MFCS, Fluigent, France) is used to impose a pres-
 91 sure P_{in} to the core fluid and a pressure P_{ext} to the external fluid.
 92 The chip is placed on the stage of an inverted microscope (DMIL
 93 LED, Leica Microsystems GmbH, Germany). Videos are recorded using
 94 a high-speed camera (Fastcam SA3, Photron, USA).

95 2.5. Coflow experiments

96 We carry out coflow experiments with miscible fluids. The
 97 reservoirs containing the external and internal fluids are connected
 98 to the pressure controller using PEEK tubes with an internal di-
 99 ameter of 0.25 mm. A fluid of viscosity μ_{in} is perfused at pres-
 100 sure P_{in} into another fluid of viscosity μ_{ext} moved at pressure P_{ext}
 101 ($\mu_{in} < \mu_{ext}$). The pressures applied to each entrance are ad-
 102 justed, varying P_{in}/P_{ext} in order to control the core flow width ϵ

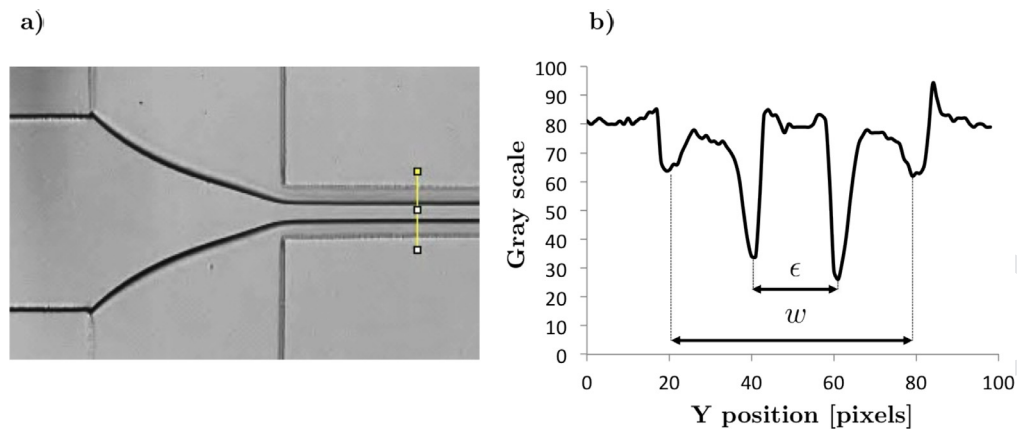


Fig. 2. (a) Photograph of a coflow of an internal flow of pure water injected into a solution of 70% of glycerol (Fluid pair A, Table 1). (b) Gray scale profile along the yellow line (Fig. 2a) used to measure the inner flow width ϵ , and the width of the channel w . (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article).

Table 1

Fluid properties for different coflows with μ_{in} (resp. μ_{ext}) as the viscosity of the inner fluid (resp. external fluid), and the viscosity contrast $\chi^{-1} = \mu_{ext} / \mu_{in}$.

Fluid pair	Internal fluid	External fluid	μ_{in} [cP]	μ_{ext} [cP]	χ^{-1}
A	Pure water	Glycerol 70%	1	30	30
B	Alginate solution	Glycerol 70%	7	30	4
C	Capsule suspension	Pure glycerol	800	1300	2

(Fig. 1b). Different fluid pairs (Table 1) are used for calibrating the flow and establishing the relationship between the flow rate ratio $\phi = q_{in} / q_{ext}$ and the width ϵ .

Coflow experiments are performed with different fluids, whose properties are summarized in Table 1. We prepare a 70% glycerol/water mixture (24397-365, VWR, France) and a 1% (w/w) low viscosity alginate (A1112, Sigma-Aldrich, St Louis, MO, USA) solution in water containing 0.9% NaCl and 0.2% Hepes. The alginate solution is agitated at least 2 days at 4°C.

For variable values of the internal and external pressures, we measure the external and internal flow rates, q_{ext} and q_{in} , in the two inlets of the flow-focusing module thanks to a flowmeter (Flowell, Fluigent, France). The value of the flow rate ratio ϕ is deduced.

Images are post-processed with the software Image J. A ROI (Region of Interest) line is drawn, containing the channel edges of the straight part (Fig. 2a). The core flow width ϵ is defined as the distance between the two minima of the gray curve plot (Fig. 2b).

2.6. Capsule flow

We prepare the capsule suspension with 20 μ L of capsules in 1 g of pure glycerol. The reservoirs containing the external and internal fluids (Fluid pair C, Table 1) are connected to the pressure controller using PTFE tubes with an internal diameter of 0.3 mm. In order to accurately capture capsule trajectories in the diverging chamber, we operated at 250 frames per second with a resolution of 1024×768 pixels, with a $10 \times$ magnification for all the videos and images. We measure the capsule speed U in the straight channel upstream of the obstacle, before any deformation, and the trajectory followed by the capsule in the divergent chamber (Fig. 4a), at different flow strengths. We define the flow strength as the product $\mu_{ext}U$. Varying the pressures P_{in} and P_{ext} modifies U , and in consequence the flow strength.

The position Y_c of the center of mass upstream of the obstacle is compared to the position of the middle of the channel $Y_0 = 0$. The off-centering κ is defined as the difference between the

two values and non-dimensionalized by the capsule diameter D , $\kappa = \frac{Y_c - Y_0}{D}$.

3. Results

3.1. Coflow at the channel entrance

Before flowing microcapsules in our device, we flowed two miscible viscous fluids to characterize the coflow in the flow-focusing module. The aim of the flow-focusing module is to center the core flow in the straight rectangular channel upstream of the obstacle. In the experiments presented in the following section, we flow capsules in the core flow and expect them to be centered onto the obstacle. But, beforehand, we carry out coflow experiments without microcapsules to understand the coflow behavior when varying the viscosity ratio $\chi = \mu_{in} / \mu_{ext}$ (Table 1).

For a given fluid pair, the viscosity ratio is fixed (Table 1), and only the inlet pressures are modified. We modify the internal pressure P_{in} keeping the external pressure P_{ext} constant, adjusting the range of variation to avoid backward surge in one or the other inlet and measure the width ϵ . We worked at variable P_{in} / P_{ext} in order to characterize the behavior of coflows and determine the relation between the width ϵ , the viscosity and flow rate ratios χ and ϕ (Fig. 3a).

The values of the internal thread width ϵ are plotted in Fig. 3 as a function of the viscosity ratio ϕ and flow rate ratio χ . It is non-dimensionalized by three different lengths α : the rectangular microchannel width w , height h and characteristic length \sqrt{hw} . The experimental results are plotted along with the ones published by Hu and Cubaud [33]. In their study conducted in a square cross-section channel ($w = h = \alpha$), they showed that the core thread width scales as:

$$\frac{\epsilon}{\alpha} = [1 + (1.5\chi^{1/2}\phi^{2/3})^{-1}]^{-1}. \quad (1)$$

We prove that the depth h , which is the smallest length in our device, does not limit the core flow width ϵ . In a square channel the three characteristic lengths are equal, and it was not obvious to know which characteristic length constrained the width ϵ . When ϵ is rescaled by $\alpha = \sqrt{hw}$, the data collapse onto the master curve defined by Eq. (1) (Fig. 3a). We then plot ϵ / \sqrt{hw} as a function of the flow rate ratio ϕ for different viscosity ratios χ and show that our experimental values agree with Hu and Cubaud [33] predictions (Fig. 3b). ϵ / \sqrt{hw} increases when the viscosity ratio χ^{-1} decreases. That means that the width ϵ can be easily deduced when we vary the pressures and flow strengths in the case when the

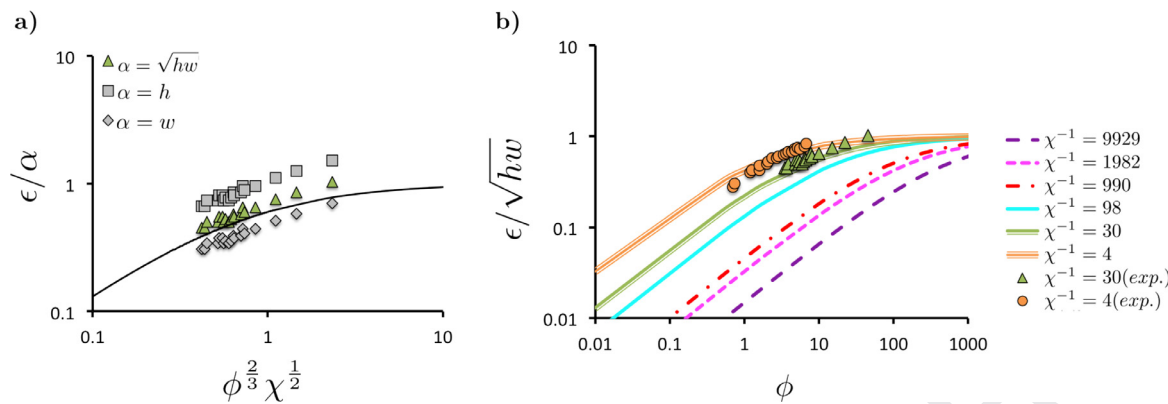


Fig. 3. The width ϵ of the core flow is expressed as a function of the flow rate ratio ϕ and the viscosity ratio χ . (a) Plot of ϵ/α for the different dimension parameters α , for the fluid pair A. Solid line represents $\epsilon/\alpha = [1 + (1.5\chi^{1/2}\phi^{2/3})^{-1}]^{-1}$. Best fit for $\alpha = \sqrt{hw}$. (b) Plot of ϵ/\sqrt{hw} as a function of ϕ for the fluid pairs A and B. Green triangles correspond to fluid pair A (water/70% glycerol mixture, $\chi^{-1} = 30$) and orange circles represent experimental data from fluid pair B (alginate/70% glycerol mixture, $\chi^{-1} = 4.28$). Solid lines represent $\epsilon/\alpha = [1 + (K_x\phi^{2/3})^{-1}]^{-1}$ ($K_x = 1.5\chi^{1/2}$) and are adapted from [33]. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article).

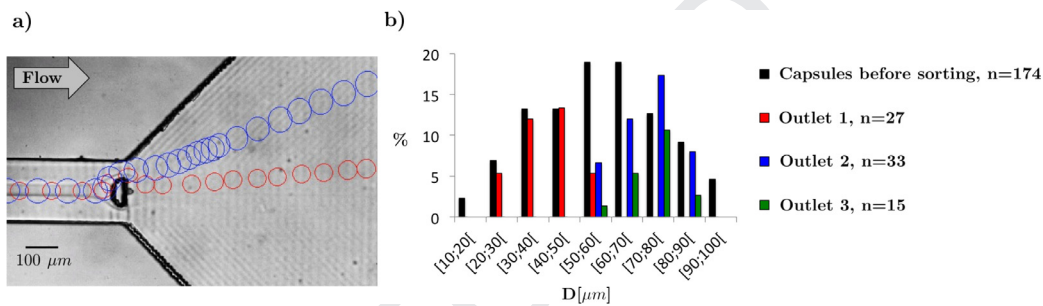


Fig. 4. (a) Trajectories of a 60 μm capsule (red) and a 80 μm capsule (blue), at various instants of time when they flow in pure glycerol (Fluid pair C, Table 1). (b) Size distribution of capsules collected at the different outlets. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article).

178 optical contrast between the 2 fluids is low or absent. In the following experiments with capsules, we apply pressures in order to
179 have values of the internal thread size ϵ smaller than the capsule diameter D .
181

182 3.2. Influence of size on the capsule trajectory

183 Prior to any flow perfusion experiment, we observe capsules
184 on a glass slide with an inverted microscope. We measure the
185 mean diameter in statics, between slide and cover, on 174 capsules
186 and found $D_0 = 60 \pm 18 \mu\text{m}$. Capsules are then flowed through a
187 50 μm gap between the wall and the obstacle, where they are
188 confined. They are then collected at the different outlets (Fig. 1a)
189 and their size distribution is determined. The external fluid is
190 pure glycerol (Fluid pair C, Table 1) with an external pressure
191 $P_{\text{ext}} = 1000 \text{ mbar}$. The internal fluid is the capsule suspension
192 (Fluid pair C, Table 1) with an internal pressure $P_{\text{in}} = 400 \text{ mbar}$.

193 We notice that larger capsules are deflected further from the
194 channel axis than smaller ones (Fig. 4a). This is confirmed by the
195 capsule size measurements at the three outlets (Fig. 4b). We found
196 an average diameter $D_1 = 39 \pm 10 \mu\text{m}$ for outlet 1 (in red, Fig. 1a),
197 $D_2 = 70 \pm 8 \mu\text{m}$ for outlet 2 (in blue, Fig. 1a) and $D_3 = 73 \pm 8 \mu\text{m}$
198 for outlet 3 (in green, Fig. 1a). These results indicate that the sys-
199 tem is able to sort micro-objects from their size. It functions as
200 a standard pinched flow fractionation device [34]. The position of
201 the center of mass of the capsule in the confined zone seems to
202 influence the trajectory followed by the capsules. The smaller the
203 capsule, the closer its center of mass from the obstacle, and the
204 smaller δ . For an identical initial position, the larger capsules pass
205 further from the obstacle and are more deflected than smaller ones

206 in the divergent chamber. The trajectory of capsules seems to be
207 sensitive to the capsule-to-obstacle distance δ , which is the only
208 modified parameter in size-based sorting.

209 3.3. Influence of flow strength on the capsule trajectory

210 The experiment is now repeated, with the same fluids
211 (Fluid pair C, Table 1), for different pressures: $P_{\text{in}} = 200 \text{ mbar}$ and
212 $P_{\text{ext}} = 1000 \text{ mbar}$ (low flow strength), and $P_{\text{in}} = 1200 \text{ mbar}$ and
213 $P_{\text{ext}} = 4500 \text{ mbar}$ (high flow strength). An increase in pressure
214 keeping the $P_{\text{in}}/P_{\text{ext}}$ ratio constant (constant core width ϵ) induces
215 an increase in the flow rates q_{in} and q_{ext} and consequently in the
216 capsule speed and forces applied to the capsule when it reaches
217 the obstacle. Depending on the capsule mechanical properties, the
218 capsule deforms more around the obstacle and its trajectory may
219 vary. The capsules produced at pH 5.9 are softer than those pro-
220 duced at pH 8 (Table 2) [25]. We can notice that the stiffness of
221 the two batches of capsules, defined as the ratio of G_s , differs only
222 by a factor of 3 ± 1.5 . Nonetheless, at constant flow strength, the
223 viscous forces push softer capsules further towards the obstacle
224 wall as they flow around it, rather than stiffer capsules. This is
225 due to the fact that viscous forces are balanced with elastic forces
226 and that the more the capsule deforms, the closer the center of
227 mass of the capsule and the obstacle (small δ). We show in Fig. 5
228 that the flow strength may have an influence on the trajectory of
229 some capsules, depending on their stiffness. Capsules prepared at
230 pH = 5.9 are less deflected at high flow strength (yellow capsule,
231 Fig. 5a) than at low flow strength (pink capsule, Fig. 5a). On the
232 contrary, capsules prepared at pH = 8 follow roughly the same tra-
233 jectory whatever the applied viscous force (Fig. 5b). For the stiffest

Table 2

Capsules produced with different pH are flowed under a pressure ratio P_{in}/P_{ext} . The velocity U is measured experimentally, and the surface shear modulus G_s arises from the experiments by Chu et al. [25]. The values of the capillary number Ca are calculated using Eq. (2).

Cond.	pH	P_{in} [mbar]	P_{ext} [mbar]	U [mm.s ⁻¹]	G_s [N.m ⁻¹]	Ca
1	5.9	267	1000	1.1 ± 0.1	0.030 ± 0.007	0.05 ± 0.01
2	5.9	1200	4500	5.0 ± 0.3	0.030 ± 0.007	0.22 ± 0.04
3	8	200	1000	0.7 ± 0.1	0.081 ± 0.026	0.01 ± 0.002
4	8	1200	4500	4.9 ± 0.6	0.081 ± 0.026	0.08 ± 0.02

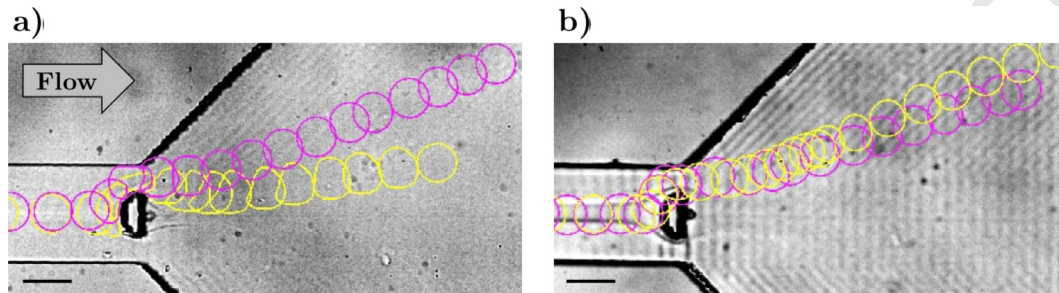


Fig. 5. Trajectory of capsules in the diverging flow chamber. Capsules were flowed at low (pink) and high (yellow) flow strengths. (a) Capsules prepared at pH 5.9. (b) Capsules prepared at pH 8. The scale bars correspond to 100 μm . (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article).

capsules (pH = 8), the trajectory is not affected by an increase in flow rates. This means that even at high pressure, the flow strength $\mu_{ext}U$ remains too small to overcome the elastic forces characterized by the 2D elastic shear modulus G_s .

4. Discussion

In the flow-focusing module at the entrance of our system, the capsule suspension forms a jet surrounded by a more viscous glycerol. The results presented in this paper show that we are able to control the width ϵ of the core flow, for a given viscosity ratio χ , by modifying the pressures applied at the entrances of our system. In the literature, the flow through flow-focusing microsystems has been abundantly studied but involves mostly the coflow of immiscible fluids, mainly for bubble [35] and droplet formation [36]. The velocity profile in the coflowing fluids differs significantly depending on whether the most viscous fluid is the internal [37] or the external one [33]. Although there are considerably fewer studies in the literature on the latter case, recent works have explored the geometry of fluid jets [33]. But no study had been conducted in rectangular channels. We show that the universal equation $\epsilon/\alpha = [1 + (1.5\chi^{1/2}\phi^{3/2})^{-1}]^{-1}$ established by Hu and Cubaud [33] in a rigid square channel for a viscosity ratio χ^{-1} between 100 and 10,000 remains valid for smaller viscosity contrasts ($\chi^{-1} = 30$ and $\chi^{-1} = 4$ in our experiments). More interestingly, the current results extend this law to soft PDMS channels with rectangular cross-section, provided the effective length scale $\alpha = \sqrt{hw}$ is used. We can imagine that for a rectangle with a larger w/h ratio, the length h would limit more effectively the width ϵ and modify the previous equation. It would be interesting to perform experiments in wider channels in order to find the limit of validity of this scaling law.

By flowing microcapsules of various sizes and mechanical properties in our device, we showed that a heterogeneous population of capsules can be sorted by size, at low flow strength. The sorting principle is similar to Pinch Flow Fractionation (PFF). In PFF systems, particles or bubbles are squeezed against a wall by an external flow. Small and large micro-objects take up distinct streamlines that can be later separated in a diverging chamber [34,38]. Unlike systems described in the literature, our device has a symmetrical design, with a constriction on each side of the obstacle.

The streamline towards which smaller objects are pushed is the centerline of the channel thus it is not located along a wall. This could allow a faster collection of small objects.

As in PFF devices, the trajectory of a capsule in the sorting device is governed by the distance δ between the obstacle and the center of mass of the capsule in the confined zone. At low flow strength, δ only depends on the size of particles to be sorted and increases with capsule diameter. Viscous forces are too small to deform capsules as they flow around the obstacle. Whatever their stiffness, δ is the capsule radius ($D/2$) and δ is maximal for capsules whose diameter is equal to the constriction width. At larger flow strength $\mu_{ext}U$, hydrodynamic forces increase and become comparable to elastic forces. In this case, the distance δ between a capsule and the obstacle no longer depends solely on capsule size, but also on capsule stiffness. Capsule sorting then depends on the capillary number:

$$Ca = \frac{\mu_{ext}U}{G_s}. \quad (2)$$

The capillary number compares viscous and elastic forces. Deformable capsules are pushed closer towards the obstacle wall (low δ) and end up following the same streamline as smaller objects. We can therefore imagine sorting microcapsules by deformability using our device. This has to be done at high capillary number Ca .

For fixed G_s , capsule deformation will only occur at large capillary number, i.e. at high flow strength $\mu_{ext}U$. We seek to determine the critical capillary number Ca_c beyond which capsule trajectory starts to depend on the mechanical properties. In earlier experiments, the 2D shear modulus G_s has been measured for several conditions of pH and reticulation time [25]. At low flow strength, pH 5.9 and 8 capsules follow the same streamline: no deformability-based sorting occurs. At high flow strength, on the other hand, soft capsules deform around the obstacle while stiff capsules do not. Using Eq. (2), we find $Ca < 0.1$ for stiff capsules and/or low flow strength (Table 2). For soft capsules, at high flow strength we find $Ca > 0.2$. This yields two different values for the distance δ between the obstacle wall and the capsule center of mass, and the two populations can be separated. Our experimental results suggest that Ca_c lies between 0.1 and 0.2. This is consistent with the numerical results found in the literature, which report on a stiff behavior at $Ca = 0.05$ and soft behavior at $Ca = 0.3$

[30]. In conclusion, a moderate increase in the 2D shear modulus G_s results in a significant modification of the trajectory when we impose high pressures in order to have $Ca < 0.1$ for a population of capsules and $Ca > 0.2$ for the other one.

The populations of rigid and soft capsules used in our experiments are polydisperse, with diameters between 55 μm and 85 μm . Many size-based separation techniques require a large size contrast between objects to be sorted, and a frankly bimodal distribution [18,34]. It is quite the opposite here: when microbeads much smaller than capsules are added to the suspension, not all of them are collected in the central outlet. This is due to the fact that they are not properly centered by the flow focusing. The distance $Y_c - Y_0$ between their center of mass and the channel axis can be as large as $\epsilon - D$. Small objects are therefore much more likely to be off-centered than objects of size $D \approx \epsilon$, which are more efficiently confined in the jet. Similarly, capsules that are much larger than the constriction have to deform to pass through the obstacle. Whatever the flow strength, they take up the whole space available and $\delta = \frac{w-\lambda}{4}$. In our system, optimal separation is thus achieved with narrow size distributions, when all objects to be sorted have a size comparable to that of the fluid thread generated by the flow focusing. In the literature, techniques based on deterministic lateral displacement or inertia have demonstrated their ability to sort bimodal populations of micro-objects. Devices relying on inertial forces to separate particles usually operate at Reynolds number (Re) between 1 and 50 [14]. In our system Re computed with particle velocity and the smallest of the 2 viscosities always remain smaller than 10^{-3} , indicating that inertial forces are negligible. We propose in this article a more sensitive device, which can sort micro-objects exhibiting moderate variability in size or deformability.

5. Conclusion

We have demonstrated that capsule sorting based on deformability and size can be achieved experimentally by using the same device at various flow rates. The present device allows us to separate and collect capsules at different outlets after sorting. It is based on the capsule ability to deform around an obstacle and to follow different trajectories depending on capsule size and stiffness. Rigid capsules follow the same trajectory, whatever the flow strength, while soft capsules are pushed towards the channel axis when the viscous forces increase. The trajectory followed by a capsule in the diffusing chamber is governed by the distance δ between the center of mass of the capsule and the obstacle in the constriction. In a polydisperse suspension, where both size and mechanical properties vary, the system can be used in two steps. A deformability-based sorting at high flow rate can follow a previous size-based separation at low flow rate, in the desired size range. This is the proof that we have developed a versatile multipurpose sorting microsystem based on a really simple design. Compared to other existing sorting devices, we demonstrate the sensitivity of our device to sort micro-objects with small size and stiffness contrasts. Further developments are expected to minimize our device dimensions and will open new perspectives to sort heterogeneous populations of cells, and help cancer diagnosis or cell differentiation.

6. Author contributions

A.L.G. conceived the experiments; D.V., O.C., P.M. and N.M. performed experiments; F.E.-L. made the capsules; D.V., A.-V.S. and A.L.G. analyzed the data; D.V., A.-V.S. and A.L.G. wrote the paper.

7. Conflict of interests

The authors declare no conflict of interests. The founding sponsors had no role in the design of the study, in the collection, analyses, or interpretation of data, in the writing of the manuscript, or in the decision to publish the results.

Acknowledgments

D.V. acknowledges financial support from the French Ministry of Research. This project has been funded by Picardy Region (FOR-PLAQ project).

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